

Boolean Algebra

1. 02-03 C2 Boolean Algebra

Simplify: $(\text{NOT } A \text{ OR } A \text{ AND NOT } B) \text{ AND } (\text{NOT } A \text{ AND } B)$

2. 02-03 C2 Boolean Algebra

Find all ordered triples that make the following expression TRUE:

$\text{NOT } A \text{ AND } C \text{ OR } B \text{ AND } (\text{NOT } (A \text{ OR } C))$

3. 03-04 C2 Boolean Algebra

Find all ordered pairs that make the following expression TRUE:

$$\bar{A} B + \overline{(A + B)}$$

4. 03-04 C2 Boolean Algebra

Simplify the following expression.

$$A(\bar{A} + B) + B(B + C) + B$$

5. 04-05 C2 Boolean Algebra

Simplify: $\overline{A(\bar{A} + B)} + B$

6. 04-05 C2 Boolean Algebra

List all the ordered pairs that make the following expression TRUE:

$$\overline{A + B} + \bar{A} B$$

7. 05-06 C2 Boolean Algebra

Simplify $\overline{\bar{A} B + A + B}$

8. **05-06 C2 Boolean Algebra**

How many ordered triples make the following expression TRUE?

$$A\bar{B} + \bar{A}C + B\bar{C}$$

9. **06-07 C2 Boolean Algebra**

Simplify completely: $\bar{A}B(A + \bar{B})$

10. **06-07 C2 Boolean Algebra**

How many ordered triples make the following expression TRUE?

$$(\bar{A} + BC)(A\bar{B} + C)$$

11. **07-08 C2 Boolean Algebra**

Simplify the following Boolean expression: $\overline{\bar{A}B} + A(\bar{B} + 1)$

12. **07-08 C2 Boolean Algebra**

Which ordered triples make the following expression TRUE? $AB + B(C + \bar{A})$

13. **08-09 C2 Boolean Algebra**

Simplify completely: $\bar{A}(A\bar{B}C + \bar{A}B\bar{C})C$

14. **08-09 C2 Boolean Algebra**

List all ordered triples that make the following expression true: $(AB + \bar{C})\overline{\bar{A}B}$

15. **09-10 C2 Boolean Algebra**

Simplify the following Boolean expression: $A(A\bar{B} + \bar{A}) + \bar{B}(\bar{A}B + A)$

16. **09-10 C2 Boolean Algebra**

Which ordered triples make the following Boolean expression FALSE?

$$AB + \bar{C}(A + \bar{B}) + \bar{B}C$$

17. **10-11 C2 Boolean Algebra**

How many ordered triples make the following Boolean expression TRUE?

$$A(\bar{B} + C) + B(\bar{A} + \bar{C})$$

18. **10-11 C2 Boolean Algebra**

Simplify the following Boolean expression: $A(\overline{A + B}) + B(\bar{A} + B)$

19. **11-12 C3 Boolean Algebra**

Simplify the following Boolean expression: $A(\bar{A}B + B) + B$

20. **11-12 C3 Boolean Algebra**

Find all ordered triples that make the following Boolean expression TRUE.

$$A(\bar{B} + C) + B(A + \bar{C})$$

21. **12-13 C3 Boolean Algebra**

Simplify the following Boolean expression: $A(\bar{A} + B) + \bar{A}B$

22. **12-13 C3 Boolean Algebra**

How many ordered triples make the following Boolean expression true?

$$(AB + \bar{C})(A + \bar{B})(BC + A)$$

23. **13-14 C3 Boolean Algebra**

Which ordered pairs make the following Boolean expression TRUE? $A(\overline{AB} + \overline{B})$

24. **13-14 C3 Boolean Algebra**

How many ordered triples make the following circuit TRUE? $\overline{A} + B\overline{C} + A(\overline{B} + C)$

25. **14-15 C3 Boolean Algebra**

Simplify the following Boolean expression: $A(\overline{BC}) + (\overline{A + B})$

26. **14-15 C3 Boolean Algebra**

Which of the following Boolean Algebra expressions are equivalent?

- a) $\overline{AB} + \overline{BC}$ b) $\overline{A} + C$ c) \overline{AC} d) 1

27. **15-16 C3 Boolean Algebra**

How many ordered pairs make the following Boolean expression TRUE?

$$\overline{A}(B + \overline{AB}) + \overline{AB}$$

28. **15-16 C3 Boolean Algebra**

Simplify the following Boolean algebra expression: $\overline{AB} + \overline{B + C} + A(\overline{B} + C)$

Solution

1. 02-03 C2 Boolean Algebra

$(\text{NOT } A \text{ OR } A \text{ AND NOT } B) \text{ AND } (\text{NOT } A \text{ AND } B) = \text{NOT } A \text{ AND } B$
 $(\text{NOT } A \text{ AND NOT } A \text{ AND } B) \text{ OR } (A \text{ AND NOT } A \text{ AND } B \text{ AND NOT } B) =$
 $\text{NOT } A \text{ AND } B \text{ OR } 0 =$
 $\text{NOT } A \text{ AND } B$

2. 02-03 C2 Boolean Algebra

$\text{NOT } A \text{ AND } C \text{ OR } B \text{ AND } (\text{NOT } (A \text{ OR } C)) = \overline{A}C + B\overline{(A+C)} \quad (0,0,1), (0,1,0), (0,1,1)$

A	B	C	$\overline{A}C$	$\overline{A+C}$	$B\overline{(A+C)}$	OR
0	0	0	0	1	0	0
0	0	1	1	0	0	1
0	1	0	0	1	1	1
0	1	1	1	0	0	1
1	0	0	0	0	0	0
1	0	1	0	0	0	0
1	1	0	0	0	0	0
1	1	1	0	0	0	0

3. 03-04 C2 Boolean Algebra

$\overline{A}B + \overline{(A+B)} = \overline{A}B + \overline{A}B = \overline{A}B \quad (0,1)$
 If $\overline{A}B = 1$ then $\overline{A} = 1$ AND $B = 1 \Rightarrow A = 0$ AND $B = 1$

4. 03-04 C2 Boolean Algebra

$A(\overline{A+B}) + B(B+C) + B = A\overline{A+B} + AB + BB + BC + B =$
 $0 + AB + B + BC = B(A+1+C) = B(1) = B \quad B$

5. 04-05 C2 Boolean Algebra

$\overline{A(\overline{A+B})} + B = \overline{A\overline{A+B}} + B = \overline{0 + \overline{A+B}} + B = \overline{\overline{A+B}} + B =$
 $\overline{\overline{A+B}} + B = \overline{\overline{A+B}} + 1 = 1 \quad 1$

6. 04-05 C2 Boolean Algebra

$$\overline{A+B} + \overline{AB}$$

(0,0) , (0,1)

A	B	A + B	$\overline{A+B}$	\overline{A}	\overline{AB}	$\overline{A+B} + \overline{AB}$
0	0	0	1	1	0	1
0	1	1	0	1	1	1
1	0	1	0	0	0	0
1	1	1	0	0	0	0

7. 05-06 C2 Boolean Algebra

Simplify

B

$$\overline{AB} + A + B = \overline{AB} + \overline{AB} = \overline{B(A+A)} = \overline{B*1} = \overline{B} = B$$

8. 05-06 C2 Boolean Algebra

The truth table is shown below. There are 6 that make the expression TRUE.

6

A	B	C	\overline{A}	\overline{B}	\overline{C}	\overline{AB}	\overline{AC}	\overline{BC}	+
0	0	0	1	1	1	0	0	0	0
0	0	1	1	1	0	0	1	0	1
0	1	0	1	0	1	0	0	1	1
0	1	1	1	0	0	0	1	0	1
1	0	0	0	1	1	1	0	0	1
1	0	1	0	1	0	1	0	0	1
1	1	0	0	0	1	0	0	1	1
1	1	1	0	0	0	0	0	0	0

9. 06-07 C2 Boolean Algebra

$$\overline{AB}(A+B) = \overline{ABA} + \overline{ABB} = 0$$

0

10. 06-07 C2 Boolean Algebra

$$(\overline{A} + BC)(\overline{AB} + C) = \overline{A}A\overline{B} + \overline{A}C + AB\overline{B}C + BCC =$$

3

$$0 + \overline{A}C + 0 + BC = C(\overline{A} + B) \Rightarrow C = 1 \text{ and } \overline{A} + B = 1$$

If $B = 1$ then $A = *$. If $B = 0$ then $A = 0$.

The triplets are $(* , 1, 1)$ and $(0, 0, 1)$

11. 07-08 C2 Boolean Algebra

$$\overline{\overline{AB}} + A(\overline{B} + 1) = \overline{A} + \overline{B} + A \bullet 1 = \overline{A} + B + A = 1 + B = 1 \quad \mathbf{1}$$

12. 07-08 C2 Boolean Algebra

First simplify: (1,1,1)

$$AB + B(C + \overline{A}) = AB + BC + \overline{A}B \quad (1,1,0)$$

$$= B(A + C + \overline{A}) \quad (0,1,1)$$

$$= B(1 + C) = B \quad (0,1,0)$$

So A = *, B = 1, C = * and the triples are (*,1,*)

13. 08-09 C2 Boolean Algebra

$$\overline{A}(\overline{A}BC + \overline{A}B\overline{C})C = \overline{A}A\overline{B}CC + \overline{A}\overline{A}B\overline{C}C = 0 + 0 = 0 \quad \mathbf{0}$$

14. 08-09 C2 Boolean Algebra

The truth table is shown below.

(0,0,0),(1,0,0),(1,1,0),(1,1,1)

A	B	C	AB	\overline{C}	$AB + \overline{C}$	\overline{A}	\overline{AB}	$\overline{\overline{AB}}$	$(AB + \overline{C})\overline{\overline{AB}}$
0	0	0	0	1	1	1	0	1	1
0	0	1	0	0	0	1	0	1	0
0	1	0	0	1	1	1	1	0	0
0	1	1	0	0	0	1	1	0	0
1	0	0	0	1	1	0	0	1	1
1	0	1	0	0	0	0	0	1	0
1	1	0	1	1	1	0	0	1	1
1	1	1	1	0	1	0	0	1	1

15. 09-10 C2 Boolean Algebra

$$A(\overline{AB} + \overline{A}) + \overline{B}(\overline{AB} + A) = A\overline{A}\overline{B} + A\overline{A} + \overline{A}B\overline{B} + \overline{A}B \quad \overline{AB}$$

$$= \overline{A}\overline{B} + 0 + 0 + \overline{A}\overline{B} = \overline{A}\overline{B}$$

16. 09-10 C2 Boolean Algebra

The truth table is as follows:

(0,1,0), (0,1,1)

A	B	C	\bar{B}	\bar{C}	AB	$A + \bar{B}$	$\bar{C}(A + \bar{B})$	$\bar{B}C$	$AB + \bar{C}(A + \bar{B}) + \bar{B}C$
0	0	0	1	1	0	1	1	0	1
0	0	1	1	0	0	1	0	1	1
0	1	0	0	1	0	0	0	0	0
0	1	1	0	0	0	0	0	0	0
1	0	0	1	1	0	1	1	0	1
1	0	1	1	0	0	1	0	1	1
1	1	0	0	1	1	1	1	0	1
1	1	1	0	0	1	1	0	0	1

Therefore, (0,1,0) and (0,1,1) make the statement FALSE.

17. 10-11 C2 Boolean Algebra

$$A(\bar{B} + C) + B(\bar{A} + \bar{C}) = A\bar{B} + AC + B\bar{A} + B\bar{C}$$

6

A	B	C	$A\bar{B}$	AC	$B\bar{A}$	$B\bar{C}$	$A\bar{B} + AC + B\bar{A} + B\bar{C}$
0	0	0	0	0	0	0	0
0	0	1	0	0	0	0	0
0	1	0	0	0	1	1	1
0	1	1	0	0	1	0	1
1	0	0	1	0	0	0	1
1	0	1	1	1	0	0	1
1	1	0	0	0	0	1	1
1	1	1	0	1	0	0	1

18. 10-11 C2 Boolean Algebra

$$\begin{aligned} A(\overline{A+B}) + B(\overline{A+B}) &= A(\overline{A}B) + \overline{A}B + BB \\ &= 0 + B(\overline{A} + 1) = B \end{aligned}$$

B

19. 11-12 C3 Boolean Algebra

$$\begin{aligned} A(\overline{A}B + B) + B &= A\overline{A}B + AB + B \\ &= 0 + B(A + 1) \\ &= B \end{aligned}$$

B

20. 11-12 C3 Boolean Algebra

$$\begin{aligned}
 A(\overline{B+C}) + B(A+\overline{C}) &= \overline{A}\overline{B} + \overline{A}C + AB + \overline{B}\overline{C} && A + \overline{B}\overline{C} \\
 &= A(\overline{B+C+B}) + \overline{B}\overline{C} \\
 &= A(1+C) + \overline{B}\overline{C} \\
 &= A + \overline{B}\overline{C}
 \end{aligned}$$

21. 12-13 C3 Boolean Algebra

$$\begin{aligned}
 A(\overline{A+B}) + \overline{A}B &= \overline{A}\overline{A} + \overline{A}B + \overline{A}B && B \\
 &= 0 + \overline{A}B + \overline{A}B = B(\overline{A+A}) = B
 \end{aligned}$$

22. 12-13 C3 Boolean Algebra

$$X = (\overline{AB+C})(\overline{A+B})(BC+A) \qquad 3$$

A	B	C	\overline{B}	\overline{C}	AB	$\overline{AB+C}$	$\overline{A+B}$	BC	$BC+A$	X
0	0	0	1	1	0	1	1	0	0	0
0	0	1	1	0	0	0	1	0	0	0
0	1	0	0	1	0	1	0	0	0	0
0	1	1	0	0	0	0	0	1	1	0
1	0	0	1	1	0	1	1	0	1	1
1	0	1	1	0	0	0	1	0	1	0
1	1	0	0	1	1	1	1	0	1	1
1	1	1	0	0	1	1	1	1	1	1

23. 13-14 C3 Boolean Algebra

$$\begin{aligned}
 A(\overline{AB+B}) &= \overline{A}\overline{AB} + \overline{A}\overline{B} = 0 + \overline{A}\overline{B} = \overline{A}\overline{B} && (1,0) \\
 \overline{A}\overline{B} = 1 &\rightarrow A=1 \wedge \overline{B}=1 \rightarrow A=1 \wedge B=0 \rightarrow (1,0)
 \end{aligned}$$

24. 13-14 C3 Boolean Algebra

$$X = \overline{A} + \overline{B}\overline{C} + A(\overline{B} + C)$$

8

A	B	C	\overline{B}	\overline{C}	\overline{A}	$\overline{B}\overline{C}$	$\overline{B} + C$	$A(\overline{B} + C)$	X
0	0	0	1	1	1	0	1	0	1
0	0	1	1	0	1	0	1	0	1
0	1	0	0	1	1	1	0	0	1
0	1	1	0	0	1	0	1	0	1
1	0	0	1	1	0	0	1	1	1
1	0	1	1	0	0	0	1	1	1
1	1	0	0	1	0	1	0	0	1
1	1	1	0	0	0	0	1	1	1

This is a tautology so all 8 of the possible inputs make it TRUE.

25. 14-15 C3 Boolean Algebra

$$A(\overline{BC}) + (\overline{A+B}) = A\overline{BC} + \overline{A+B} = A\overline{BC} + \overline{A}\overline{B} = A\overline{BC} + \overline{A}\overline{B} = \overline{A}\overline{B}(C+1) = \overline{A}\overline{B}$$

$\overline{A}\overline{B}$

26. 14-15 C3 Boolean Algebra

a. $\overline{AB} + \overline{BC} = \overline{A} + \overline{B} + \overline{B} + \overline{C} = \overline{A} + B + \overline{B} + C = \overline{A} + 1 + C = 1$

a and d

b. $\overline{A} + C$ c. $\overline{AC} = A + \overline{C}$ d. 1

27. 15-16 C3 Boolean Algebra

$$\begin{aligned} \overline{A}(B + \overline{AB}) + \overline{AB} &= \overline{A}B + \overline{A}A\overline{B} + \overline{A} + \overline{B} = \overline{A}B + 0 + \overline{A} + \overline{B} \\ &= \overline{A}(B+1) + \overline{B} = \overline{A} + \overline{B} = \overline{AB} \end{aligned}$$

3

If $\overline{AB} = 1$, then $AB = 0$. So $A = 0 \vee B = 0$. Therefore 3 ordered pairs make the expression TRUE. (0,1), (1,0), (0,0)

28. 15-16 C3 Boolean Algebra

$$\begin{aligned} \overline{AB} + \overline{B+C} + A(\overline{B} + C) &= \overline{A} + \overline{B} + \overline{B}\overline{C} + \overline{A}\overline{B} + AC \\ &= A + AC + \overline{B} + \overline{A}\overline{B} + \overline{B}\overline{C} \\ &= A(1+C) + \overline{B}(1+A+\overline{C}) \\ &= A + \overline{B} \end{aligned}$$

$A + \overline{B}$